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A HIGH-PRESSURE SHOCK TUBE STUDY OF HYDROGEN AND AMMONIA ADDITION TO NATURAL GAS FOR REDUCED CARBON EMISSIONS IN POWER GENERATION GAS TURBINES

by

MICHAEL PIERRO B.S. University of Central Florida, 2020

A thesis submitted in partial fulfillment of the requirements for the degree of Master of Science in the Department of Mechanical and Aerospace Engineering in the College of Engineering and Computer Science at the University of Central Florida Orlando, Florida

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ABSTRACT

Ignition delay times from undiluted mixtures of natural gas (NG)/H2/Air and NG/NH3/Air were measured using a high-pressure shock tube at the University of Central Florida. The combustion temperatures were experimentally tested between 1000-1500 K near a constant pressure of 25 bar. Mixtures were kept undiluted to replicate the same chemistry pathways seen in gas turbine combustion chambers. Recorded combustion pressures exceeded 200 bar due to the large energy release, hence why these were performed at the high-pressure shock tube facility. The data is compared to the predictions of the NUIGMech 1.1 mechanism for chemical kinetic model validation and refinement. An exceptional agreement was shown for stoichiometric conditions in all cases but strayed at lean and rich equivalence ratios, especially in the lower temperature regime of H² addition and all temperature ranges of the baseline NG mixture. Hydrogen addition also decreased ignition delay times by nearly 90%, while NH³ fuel addition made no noticeable difference in ignition delay time. NG/NH₃ exhibited similar chemistry to pure NG under the same conditions, which is shown in a sensitivity analysis, demonstrating hydrogen chemistry to be dominant in NG/H² mixtures and hydrocarbon chemistry to be dominant in NG/NH³ mixtures. The reaction $CH_3 + O_2 = CH_3O + O$ is identified and suggested as a possible modification target to improve model performance. Increasing the robustness of chemical kinetic models via experimental validation will directly aid in designing next-generation combustion chambers for use in gas turbines, which in turn will greatly lower global emissions and reduce greenhouse effects.

to Mom, Dad, and Megan Pierro

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CHAPTER 1: INTRODUCTION

For the past century, fossil fuel combustion has driven the global economy and led the energy sector as the main electricity provider. Although natural gas (NG) has replaced coal as a cleaner burning fuel, carbon dioxide (CO_2) is still a main product of combustion. As part of the worldwide initiative to decrease carbon emissions, studies into hydrogen (H_2) and ammonia (NH_3) combustion for uses in gas turbines have accelerated. Both H_2 and NH_3 are favorable as NG replacements due to their carbon-free emissions; however, both entail major challenges. The storage, transportation, and flame stability of these fuel alternatives has yet to be properly controlled. There are also concerns about the tangibility of these fuels as they both require methane steam reforming to be produced, but Haugen *et al*. have shown methods of capturing the CO² produced during the reforming process [1].

Hydrogen is a favorable fuel because it does not produce carbon nor fuel-nitrogen oxide (NO_x) emissions (unlike ammonia) when burned with pure oxygen $(O₂)$ but draws major issues with its storage, transportation, and high reactivity. H_2 is also prone to flame flashback because of its high burning velocity [2, 3], which causes the flame to propagate upstream of the designed location in the combustor. Conversely, blowout is a common issue encountered with $NH₃$ flame stability due to its slower chemical reactions $[4, 5]$, where NO_x emission levels are optimally low. When combusted, L-NH₃ has a higher volumetric energy density than L-H₂, but any ammonia combustor must also be able to confidently have near-complete combustion to prevent leftover toxic NH₃ molecules in the exhaust, or "ammonia slip". On top of that, nitrous oxide (N_2O) , another product from NH³ combustion, has been said to potentially have a much larger impact on the climate than $CO₂$ itself [6] but can be effectively mitigated to some extent using selective

catalytic reduction (SCR) [7]. Ammonia can, however, be utilized to act as a hydrogen carrier. Through the reverse Haber-Bosch process, a heated catalytic surface (most likely ruthenium or iron) can be used to break up $2NH_3 \Leftrightarrow N_2 + 3H_2$ [8]. Additionally, there are already existing L-NH³ pipelines that have proven reliable for decades and could be used for ammonia transportation [9, 10].

The combustion instabilities can be offset when premixed blends of NG/NH_3 or NG/H_2 are utilized, providing a stable and efficient flame with lowered carbonous and nitrogenous emissions while making minimal modifications to existing NG turbines [11, 12]. While flame speeds and emissions are more optimal using blends solely of H_2/NH_3 , the infrastructure required to swap existing NG pipelines and turbomachinery would be an immensely expensive and time-consuming operation. Several studies have been performed to measure the combustion characteristics of these blends to find an optimum equivalence and fuel ratio during turbine operation, as outlined by Chai *et al*. [13]. By use of a robust chemical kinetic model, these fuel blends can be optimized using computational fluid dynamics (CFD) rather than experimental data. The scope of this project aims to experimentally study the ignition delay times (IDTs) of undiluted NG/NH3/Air and NG/H2/Air mixtures at the relevant pressures and temperatures (25 bar, 1000-1500 K) in order to validate and refine the current chemical kinetic mechanisms.

CHAPTER 2: LITERATURE REVIEW

While much work has been performed over the past decade to study NG/H₂ mixtures, and few recent studies have looked into NG/NH³ blends, little have tested undiluted mixtures at the temperatures and pressures experienced in gas turbine combustors. Previous ignition delay time measurements of H² addition into methane (CH4) at elevated pressures by Gersen *et al*. demonstrated that mixtures containing less than 20% H₂ had a modest effect on ignition whereas 50% addition dramatically decreased IDT [14]. More shock tube studies by Herzler and Naumann and Huang *et al*. both found that chemical kinetic model performance decreased with increasing addition of H₂ [15, 16]. De Vries and Petersen [17] studied undiluted lean (Φ =0.5) mixtures of pure NG/H² mixtures near the same conditions presented in the current study and found weak ignition to be prevalent. Weak ignition, in comparison to strong ignition, is a common issue with high-fuel-containing mixtures in the shock tube. As noted by De Vries and Petersen [17], there must be a distinction made between these two ignition events to properly build a chemical kinetic model. Similar work done by Laich *et al*. [18] also showed non-idealities for high-fuel-loaded mixtures of methane at lower temperatures near 15 bar.

Shock tube studies of methane addition into ammonia near 40 bar by Shu *et al*. revealed that increasing methane concentrations increased reactivity but conversely increased both CO and NO emissions [19]. Work by Baker *et al*. [20] has also already been performed at lower pressures and higher temperatures using diluted mixtures as an initiative to develop a robust $NG/H₂/NH₃$ model entitled UCF 2022. Similarly, mechanism development and reduction by Li *et al*. specifically targeted $CH_4/H_2/NH_3$ mixtures however does not encompass alkanes larger than C_2 [21]. This paper seeks to extend the pressure range of the chemical kinetic models as well as validate the ignition properties for undiluted mixtures of H² and NH³ addition to NG.

CHAPTER 3: EXPERIMENTAL METHODS

3.1 Shock Tubes

Mixtures were shock-heated and auto-ignited using a high-pressure shock tube at the University of Central Florida's (UCF) High-Pressure Extended Range Shock Tube for Advanced Research (HiPER-STAR) facility [22]. A shock tube allows for consistent replication of combustion studies through velocity control of the generated shock. The tube is separated into two sections. The high-pressure section (referred to as the driver) is filled with a non-reactive gas, in this case, a tailored mixture of ultra-high purity (Nexair, 99.999%) helium (He) and ultra-high purity (Nexair, 99.999%) nitrogen (N_2) until the pre-scored aluminum diaphragm between the two sections is ruptured at the pre-determined break pressure. The large pressure difference following the diaphragm rupture forms a shock wave, which travels downstream of the shock tube. It should be noted that the driver gas tailoring is not used to extend test time (as commonly referred to in shock tube literature) but instead to target specific experimental pressure and temperature. The low-pressure section of the shock tube is referred to as the driven section, which contains the mixture of study and is heated initially by the incident shock wave, and then once again after the shock wave reflects off the end wall of the shock tube. The secondary heating from the reflected shock wave brings the volume behind the shock to the desired temperature and pressure of the study at stagnant conditions. Temperature and pressure measurements were calculated from an inhouse Python ideal and real gas 1-D frozen shock equation solver (PyRGFROSH) [23] using the shock velocity from the time intervals between five piezoelectric sidewall dynamic pressure transducers downstream of the shock tube (shown in [Figure 1\)](#page-16-0). For the current study, the ideal gas solver was used. These were then validated by the State 5 pressure recording.

Figure 1:Visual representation of shock wave propagating downstream of the shock tube with pressure transducers in their approximate locations. Subscript 1 refers to the state properties before the arrival of the incident shock wave. State 5 is the test conditions after the reflected shock wave.

Figure 2: Distance-time (x-t) diagram of the shock tube, demonstrating the movement of shock waves during an experiment

3.2 Mixture Preparation

Mixtures were made using the partial pressures (assuming Dalton's law) calculated from mole fractions of balanced chemical equations and then pre-mixed in a magnetically stirred highpressure mixing tank. As noted earlier, the mixtures were undiluted to replicate the chemistry during realistic gas turbine conditions, meaning the only gas constituents were fuel and synthetically made air. In all cases, the $O_2:N_2$ ratio was kept constant at 1:3.76. The NG mixture was a pre-made blend of 97.37614% CH4, 2.25% C2H6, 0.077% C3H8, 0.00506% C4H10, 0.242% N_2 , and 0.0498% CO_2 , which was primary standard certified by Nexair. It is important to note that larger quantities of higher-order hydrocarbons can accelerate the ignition process and change reaction pathways therefore, lower concentrations of these were used in the study as an analog to industrial applications [24, 25]. Ultra-high purity (99.999%) O_2 and N_2 were also supplied by Nexair. A list of the mixture constituents is formatted below in [Table 1.](#page-18-1) Hereafter, mixtures will be referred to by their designated names from the table. $NH₃$ is also known to adsorb into the stainless-steel shock tube [26], which could disrupt the purity of the mixture; however, when high molar concentrations of NH³ are used, it has been experimentally determined by Pochet et al. that any adsorbed ppm quantities are not enough to have an effect on IDT [27]. Furthermore, the facility mixing tank is Teflon coated to further reduce this phenomenon.

	NG	H ₂	NH ₃	Equivalence ratio (Φ)
Mix ₁	$\mathbf{1}$	$\overline{0}$	$\overline{0}$	1.0
Mix 2	0.5	0.5	$\overline{0}$	1.0
Mix 3	0.5	$\boldsymbol{0}$	0.5	$1.0\,$
Mix 4	$\mathbf{1}$	$\overline{0}$	$\overline{0}$	0.5
Mix 5	0.5	0.5	$\boldsymbol{0}$	0.5
Mix 6	0.5	$\boldsymbol{0}$	0.5	0.5
Mix 7	$\mathbf{1}$	$\overline{0}$	$\overline{0}$	2.0
Mix 8	0.5	0.5	$\boldsymbol{0}$	2.0
Mix 9	0.5	$\boldsymbol{0}$	0.5	2.0

Table 1: Fuel fraction of tested mixtures

3.3 IDT Measurements

All measurement devices are located at the test section of the shock tube, which is located 1 cm in front of the driven section endwall. Ports containing sapphire windows are used to allow optical access. Strong ignition IDTs (τ_{ign}) were determined by the max peak in OH* chemiluminescence, starting from the point of max pressure rise in PCB 5 from the reflected shock wave (defined as "time-zero"), as shown in [Figure 3.](#page-19-0) It should be noted that a secondary peak in the OH^{*} trace is seen to be higher than the reported τ_{ign} in the case of [Figure 3,](#page-19-0) which was present in a few ignition traces. This peak is not considered to be the "max peak" due to it coalescing with a post-detonation oscillation in the pressure trace. In all experiments, the OH* detector is radially located 180° from PCB 5, hence why oscillations in both traces are generally in phase with each other. The post-detonation environments in undiluted mixtures are very dynamic and can create oscillations in the diagnostics, such as these.

Figure 3: Homogenous pressure trace from Mix 2 using OH* max species concentration for determination of IDT.

The reasoning for calculating time-zero at the max pressure rise in PCB 5 from the reflected shock wave is that a bifurcated shock wave can be observed in the pressure signal due to measurements collected from sidewall-mounted transducers as opposed to endwall-mounted. Although the pressure nearest the wall is measuring the pressure caused by the boundary layer, it is assumed the core flow of the reflected shock wave is at the State 5 conditions, which is validated once the signal equilibrates several microseconds afterward. This concept is fully explained in detail by Petersen and Hanson [28]. Non-homogenous IDTs were not reported in this study due to uncertainty in the IDT determination, which was observed to be mixture independent in the lower temperature region, as discussed in Chapter 3.5.

As reported by Petersen [29], reporting IDTs from sidewall-mounted diagnostics for undiluted shock tube mixtures will make them slightly faster than endwall-based diagnostics due to strong ignition events volumetrically igniting the entire test section region. In these cases, the discrepancy comes from the time-zero measurement since the reflected shock wave arrives at the sidewall several microseconds after it departs from the endwall. In dilute mixtures cases, this phenomenon is not seen since strong ignition events generally do not occur, hence, sidewallmounted diagnostics are not artificially faster because the ignition originates from the endwall rather than volumetric test section ignition. This reporting difference is considered to be both mixture and facility dependent. As said by Shu *et al*. [30], pure ammonia is slow to react and therefore strong ignition events are not seen. In addition, some facilities collect sidewall IDTs at different axial locations, affecting the time reporting difference when volumetric test section ignition occurs. In the case of this study, the shock tube was not capable of collecting endwall IDTs and therefore the variable endwall location was set to be 1 cm from the sidewall diagnostics to collect as close to the endwall as possible and reduce the time difference between endwall reported IDTs for strong ignition events. The time-zero difference was extrapolated using the reflected shock wave velocity from PyRGFROSH and calculated for each experiment to be between 25-27 µs, artificially making IDTs faster by this amount if volumetric ignition occurs in the test section region. For IDTs reported above 170 µs, this difference is within the uncertainty range however for higher temperature points with IDTs below this value, the uncertainty is increased to 16-38%.

3.4 Reaction Mechanism

Primarily a hydrocarbon-based chemical kinetic model, the NUIGMech 1.1 [31] contains 2845 species and 11260 reactions with alkanes up to C_7 . The model encompasses all of the species used for the NG mixture in this study (up to C_4) while also containing an NO sub mechanism by Glarborg *et al.* [32] for NH₃ chemistry. Comparisons to the mechanism were made by applying the State 5 conditions to a constant volume 0-D batch reactor and simulated using a Cantera [33] Python code using the same IDT determination method as in the experimental calculations.

Following the experimental data is a sensitivity analysis of selected temperature points and mixtures performed in ANSYS CHEMKIN PRO 2022 R2 software [34]. Each sensitivity analysis was taken during the time at which the fuel was half consumed. In the case of blended mixtures, the slowest reacting of the two fuels was used in order to fully capture the synergistic chemistry. For the NG mixtures, the decomposition of CH⁴ was used. A sensitivity analysis can help determine which chain reactions are prominent in the ignition sequence. When the sensitive reactions are compared across different temperature points and mixtures, conclusions about key chemistry differences can be inferred. In the case of this study, a sensitivity analysis is used to compare chemistry H₂ and NH₃ addition to baseline NG. The ANSYS CHEMKIN PRO sensitivity coefficients (*S*) are calculated using the methodology described by Neupane *et al*. [35],

$$
S = \left(\frac{dX(t)}{dk_i}\right)\left(\frac{k_i}{X(t)}\right) \tag{1}
$$

where *X* is the species mole fraction over time and k_i is the ith reaction rate. *S* is then normalized (S_N) to the maximum sensitivity (S_{max}) of all sensitive reactions to the mixture using,

$$
S_N = \frac{S_i}{S_{max}}\tag{2}
$$

3.5 Pre-ignition Phenomenon

A common gas dynamic phenomenon experienced in shock tubes is a boundary layer forming while the reflected shock passes through the State 2 conditions. The boundary layer causes the reflected shock to bifurcate and form two oblique shocks on the leading and -trailing edges nearest the walls. Fundamental research by Mark [36] and Hollyer [37] found that the bifurcation is directly dependent on the specific heat ratio (γ) of the gaseous mixture. Monatomic gases, typically used in diluted shock tube mixtures, do not exhibit a boundary layer large enough to affect the shock wave because of their larger γ. However, diatomic and polyatomic mixtures, which have lower γ values, bifurcate the shock wave and create a turbulent boundary layer. Yamashita *et al*. [38] performed advanced shock tube CFD and showed the triple point at which the oblique shocks meet the normal shock to be hotter than the core flow. The hot triple point then caused "hot spots" in the turbulent boundary layer, which are small pockets of high-temperature differences, as much as 50 K more for an 850 K State 5 temperature. The bifurcation also grows as the shock travels further, increasing the size of the localized hot spot in the triple point. Due to the low activation energy of the high-fuel mixture, the hot spot could locally ignite that region before the core flow. This is a non-ideal pre-ignition phenomenon that onsets the rest of the ignition, thus the mixture is not igniting at the theoretical post-shock temperature (T_5) .

Figure 4: Non-homogenous pressure trace from Mix 2. Observed non-idealities also present in OH* emission trace.

Since the mixtures studied in this work are being oxidized in air and undiluted, (all the molecules are diatomic or polyatomic) the resulting reflected shock wave experiences bifurcation, making it difficult to homogeneously ignite in the low-temperature region. An example of a nonideal ignition trace is shown in [Figure 4,](#page-23-0) which very clearly exhibits pressure and emissions signal rise before strong ignition (circled in red). Determination of the IDT cannot be well defined due to strong ignition occurring roughly 325 µs after pre-ignition onset. This phenomenon was seen in the low-temperature regions for all mixtures except for the rich conditions.

To prevent preignition, temperatures below 1070 K attempted to employ the constrained reaction volume (CRV) stage-filling approach refined by Hanson et al. at Stanford University [39- 41] (displayed in [Figure 5\)](#page-24-0). In the CRV stage-filling technique, the fuel mixture is first added at a lower partial pressure. After that, non-reactive stage-filling gas is slowly introduced near the diaphragm of the shock tube until the correct total P_1 is achieved, compressing the fuel mixture at the test section and preventing non-localized ignition. The stage-filling gas should closely match the specific heat ratio of the fuel mixture, as well as the average molecular weight of the mixture. This technique required characterization of the diffusivity between the two gases in order to prevent the stage-filling gas from diluting the fuel mixture. Preliminary tests were performed to determine if the process is viable using $CH_4/O_2/Ar$ mixtures stage-filled with argon (Ar). The total fill time was around 7 minutes.

Figure 5: Illustration of the shock tube driven section CRV stage-filling. Subscript 1 refers to the state properties before the arrival of the incident shock wave. State 5 is the test conditions after the reflected shock wave.

Defined by Hanson et al., L_1 , the initial length of the test gas before compression, is determined by using:

$$
L_1 = L_5 \frac{\rho_5}{\rho_1} = L_5 \frac{P_5 T_1}{P_1 T_5}
$$
 (3)

where the density ratio can be related to temperature and pressure relations using the ideal gas law. Substituting ideal shock equations for the pressure and temperature relations for a given Mach number:

$$
\frac{P_5}{P_1} = \left\{ \frac{2\gamma M_1^2 - (\gamma - 1)}{\gamma + 1} \right\} \left\{ \frac{(3\gamma - 1)M_1^2 - 2(\gamma - 1)}{(\gamma - 1)M_1^2 + 2} \right\} \tag{4}
$$

$$
\frac{T_5}{T_1} = \frac{\{2(\gamma - 1)M_1^2 + (3 - \gamma)\}\{(3\gamma - 1)M_1^2 - 2(\gamma - 1)\}}{(\gamma + 1)^2 M_1^2}
$$
\n(5)

and by specifying an optimal L_5 of approximately 4.5 cm, L_1 can be related to the mixture pressure using:

$$
P_{1\text{test gas}} = \frac{L_1 P_{1\text{total}}}{x} \tag{6}
$$

where *x* is the distance from the end wall to the fill location.

Diffusivity between the test gas and the stage-filled gas is inevitable but can be characterized with uncertainty if the fill-time is optimized to prevent turbulent mixing and gasstratification, documented by Susa *et al.* [42]. Initial testing of 4% CH₄ / 8% O₂ / 88% Ar stagefilled with Ar [\(Figure 7\)](#page-27-0) was attempted and showed a discrepancy in the post-reflected shock pressure when compared to the ideal shock equations' calculated pressure. A conventionally filled mixture with double the amount of Ar $(2.13\% \text{ CH}_4 / 4.26\% \text{ O}_2 / 93.62\% \text{ Ar}, \text{Figure 8})$ is shown except with the ideal shock equations' P_5 calculation performed as if there was no extra Ar addition, leading to a similar but exaggerated discrepancy shown in the stage-filled experiment [\(Figure 7\)](#page-27-0).

The trace in [Figure 6](#page-26-0) is the same mixture as the stage-filled in [Figure 7,](#page-27-0) except conventionally filled. PCB 5 is in good agreement with the ideal shock equations' calculations, which is normally seen in the facility experiments. A possible characterization to stage-filling that will be explored is to back-calculate P_5 to determine the amount of stage-filled gas that diluted the test mixture. From there, the uncertainty would be determined, however this is not considered to

be a trustworthy method and therefore the CRV stage-filling method was concluded not to be sufficient for high-pressure shocks and will not be employed for these experiments.

Figure 6: Conventionally filled pressure trace (black) showed to match theoretical calculated P₅ (red).

Figure 7: Stage-filled pressure trace (black) showed to deviate from theoretical calculated P₅ (red).

Figure 8: Conventionally filled pressure trace of a mixture containing double the amount of Ar (black) shown to deviate from theoretical calculated P_5 (red). FROSH P_5 was calculated without doubling Ar and the pressure trace deviates similar to the stage-filled mixture thus indicating that the stage-filled mixture was rather completely mixed.

CHAPTER 4: EXPERIMENTAL RESULTS AND CHEMICAL KINETIC MODEL PERFORMANCE

4.1 IDT Analysis

The IDT measurements presented in Figures 9-11 were taken near 25 bar between a temperature range of 1000-1500 K. All collected points are listed in [Table 2.](#page-28-2) Baseline mixtures of pure NG were taken to compare the addition of H_2 and NH_3 at each equivalence ratio. The NUIGMech 1.1 mechanism was used for simulations of each mixture at 25 bar (solid line) to show the logarithmic ignition trend across the entire temperature range. The experimental data are solidfilled points on the plot with a calculated 15% uncertainty, which is calculated from the uncertainty in the shock velocity and further explained by Urso *et al*. [22]. Hollow points represent the NUIGMech 1.1 simulated at the exact experimental pressure as the accompanying solid-filled experimental point, as some data points may be slightly above or below 25 bar. The mixtures are named based on their assigned "Mix" number in [Table 1.](#page-18-1)

Mix	P [bar]	T[K]	IDT $[\mu s]$
$\mathbf{1}$	22.1	1317	659
	23.2	1349	441
	25.2	1350	396
	24.3	1378	317
	24.3	1388	260
	26.2	1437	156
$\overline{2}$	24.9	1091	993

Table 2: Experimental IDT data for each mixture with pressure and temperature measurements

Figures 9-11 are fuel-independent IDT plots of baseline NG, NG/H2, and NG/NH3, respectively, comparing the changing equivalence ratio effects on ignition. Stoichiometric conditions are black circles, rich conditions are red squares, and lean conditions are blue triangles, which are consistent for this set of plots.

[Figure 9](#page-34-0) shows the IDTs for pure NG mixtures at different equivalence ratios. In general, experimental IDTs tend to decrease with increasing temperature. At 1437 K, the IDT was found to be 156 μ s, though a decrease in ~120 K increases the IDT to ~650 μ s at 1317 K and Φ=1.0. For Φ =0.5, IDT is found to be 138 µs at 1435 K, while at 1304 K, it is 640 µs. Previous studies [43] indicate that dilute hydrocarbon mixtures ignite faster at fuel-lean conditions $(\Phi=0.5)$ while slowing down ignition at fuel-rich conditions $(\Phi=2.0)$. However, in undiluted conditions, only a negligible difference is observed in IDTs for lean and stoichiometric conditions. This is primarily due to the higher concentration of fuel in stoichiometric cases than in lean cases. At high temperatures (~ 1400 K), the fuel-rich mixture (Φ =2.0) ignites faster than its Φ =1.0 and Φ =0.5 counterparts and shows similar IDTs $(598 \mu s$ at $1317 \text{ K})$ at lower temperatures as evident from [Figure 9.](#page-34-0) Similar observations are made with $NG/H₂$ mixtures [\(Figure 10\)](#page-34-1), where the lean case shows the longest IDTs followed by stoichiometric and rich cases. Negative temperature coefficient (NTC) behavior was not seen in any case, unlike the results found by De Vries and Petersen [17] however, their study was in the lower temperature region where NTC is more commonly observed with CH⁴ [44]. As mentioned in Chapter 3.2, concentrations of higher-order hydrocarbons were exceptionally low in the NG mixture and therefore the pure NG mix was expected to behave close to pure methane. This conclusion for NTC behavior is similarly drawn since NTC of large alkanes occurs near the same temperature region of CH⁴ [44].

Model agreement is excellent for stoichiometric conditions (apart from Mix 1), supporting that undiluted mixtures do not have a significant effect on ignition chemistry. De Vries and Petersen [17] similarly showed that ignition with methane does not change if an Ar bath gas is replaced with N_2 , however, NO pathways for air-breathing engines using NH_3 can be affected if excess N_2 is present in the combustion, and ultimately affect emissions and ignition. For these cases, the N_2 chemistry from the NO sub-mechanism predicts very accurate IDTs in all mixture conditions. Baseline NG ignition did not change with changing equivalence ratios [\(Figure 9\)](#page-34-0), whereas NG/H₂ mixtures auto-ignited faster in rich conditions and slowed in the lean conditions, which the model accurately predicts [\(Figure 10\)](#page-34-1). NG/NH₃ experimental data shows that changing the equivalence ratio did not affect ignition, similar to pure NG. However, the model predicted lean conditions to be quicker and rich conditions to ignite slower [\(Figure 11\)](#page-35-1).

When increasing or decreasing the equivalence ratio, pure NG IDTs became faster than the model predictions at all temperatures while NG/H² were also slightly faster than the model at lower points in the temperature range. Additionally, NG/H² ignition shows to trend linearly with changing temperature for stoichiometric and rich cases but non-linearly for lean conditions, which the model fails to capture.

Figure 9: Experimental baseline NG IDTs compared to chemical kinetic model. (Mix 1 is at Φ =1.0, Mix 4 is at Φ =0.5, and Mix 7 is at Φ =2.0).

Figure 10: Experimental NG/H² IDTs compared to chemical kinetic model. (Mix 2 is at Φ=1.0, Mix 5 is at Φ =0.5, and Mix 8 is at Φ =2.0).

Figure 11: Experimental NG/NH₃ IDTs compared to chemical kinetic model. (Mix 3 is at Φ =1.0, Mix 6 is at Φ =0.5, and Mix 9 is at Φ =2.0).

4.2 Effect of Hydrogen and Ammonia Addition

For this section, baseline NG mixtures are black circles, mixtures with NH₃ addition are red squares, and H2-containing mixtures are blue triangles. [Figure 12](#page-36-0) shows stoichiometric conditions, [Figure 13](#page-37-0) compares lean conditions, and [Figure 14](#page-37-1) compares rich conditions.

Similar to the analysis made by Baker *et al.* [20], H₂ addition very significantly increases the reactivity of the mixture, thus experiencing much quicker IDTs. Hydrogen addition decreases the IDT by approximately 90% for stoichiometric conditions [\(Figure 12\)](#page-36-0), 86% for lean conditions [\(Figure 13\)](#page-37-0), and 89% for rich conditions [\(Figure 14\)](#page-37-1). Conversely, NH³ addition shows little effect on the ignition when compared to the baseline. These observations can be attributed to dominating H² chemistry for NG/H² mixtures whereas NG/NH³ mixtures are dominated by hydrocarbon chemistry. Further analysis of the chemistry between these reactions is found in Chapter 4.4. Baker *et al.* [20] also noted that NH₃ greatly decreased the reactivity of the mixture in their study when compared to baseline NG. However, the NG mixture used contained larger amounts of higher order hydrocarbons, whereas this study only contains ppm quantities \langle <770 ppm C₃H₈ and <51 ppm C_4H_{10} , hence supporting that the higher order alkanes play little role in the ignition behavior when in small quantities. Baker *et al*. [20] similarly suggested that the larger hydrocarbons initially formed OH radicals faster than the rest of the reactants.

Figure 12: Experimental stoichiometric (Φ =1.0) IDTs compared to chemical kinetic model. (Mix 1 is baseline NG, Mix 2 is NG/H2, and Mix 3 is NG/NH3).

Figure 13: Experimental lean (Φ=0.5) IDTs compared to chemical kinetic model. (Mix 4 is baseline NG, Mix 5 is NG/H2, and Mix 6 is NG/NH3).

Figure 14: Experimental rich (Φ=2.0) IDTs compared to chemical kinetic model. (Mix 7 is baseline NG, Mix 8 is NG/H2, and Mix 9 is NG/NH3).

4.3 Sensitivity Analysis

Sensitivity analyses between mixtures are shown in Figures 15-18 to find shared reactions that are most prominent to ignition. As noted in Chapter 3.4, each sensitivity analysis was performed using OH formation rather than a fuel decomposition due to the blending from multiple fuels. Although this does not affect the sensitivity analysis, it does change the perspective of the sensitivity coefficients. Therefore, positive sensitivity coefficients are indicative of ignitionpromoting reactions, while negative sensitivity coefficients are ignition-inhibiting reactions.

Lower temperature pure NG ignition for stoichiometric conditions is mainly dominated by the CH³ reactions,

$$
CH_3 + O_2 = CH_2O + OH \tag{R114}
$$

$$
CH_3 + HO_2 = CH_3O + OH \tag{R122}
$$

as shown in [Figure 16.](#page-40-1) The breakdown of the C-H bond also frees an H atom and promotes the chain-branching reaction,

$$
O_2 + H = O + OH \tag{R10}
$$

which is an elementary reaction in the hydrocarbon ignition process. (R10) is also very sensitive to NG/H₂ ignition because of the H-H bond separation in H₂. This reaction is then expedited due to two readily available H atoms rather than the one from C-H. The early onset of (R10) consumes available O_2 and inhibits methyl oxidation, leading to hydrocarbon pyrolysis rather than oxidation. With no free O_2 molecules leftover H atoms bond together, leaving large amounts of H_2 in the products of the combustion. This pattern was common for all NG/H² mixtures, especially for fuelrich conditions.

Unlike the H_2 addition, NH_3 does not heavily affect the sensitive reactions to OH. Many of the commonly shared reactions of pure NG and NG/NH³ in [Figure 18](#page-41-1) have similar effects on ignition, indicating that hydrocarbon chemistry is dominant. (R10), (R114), and (R122) are still the most prominent reactions however mainly from C-H breakdown in these cases. This similarly causes pyrolyzation of nitrogen chemistry and creates free H atoms from N-H separation, thus still leaving ample amounts of H_2 in the combustion products.

As discussed earlier in Chapter 4.1, NG/NH₃ chemistry is affected by the presence of air $(N₂)$ in replacement for Ar. During the combustion, high-temperature thermal NO begins through the chain reaction,

$$
N + O_2 = NO + O \tag{R10467}
$$

through which,

$$
NO + HO2 = NO2 + OH
$$
 (R10517)

is initiated and promotes OH radical production. [Figure 17](#page-41-0) shows (R10517) to be an ignitionpromoting reaction for stoichiometric mixtures of NG/NH3. Although this reaction sequence is also driven by fuel NO from ammonia, energy is first required to break N-H bonds to get free NH molecules whereas an N-N bond separation readily frees two N atoms from N_2 in air. In the case of these mixtures, NH molecules from pyrolyzed NH³ and separated N-N bonds are both contributing to NO in (R10467).

Figure 15: Stoichiometric NG/H² sensitivity analysis at 1150 K and 1250 K.

Figure 16: Stoichiometric NG/H² sensitivity analysis at 1250 K compared to baseline NG.

Figure 17: Stoichiometric NG/NH³ sensitivity analysis at 1250 K and 1400 K.

Figure 18: Stoichiometric NG/NH³ sensitivity analysis at 1250 K compared to baseline NG.

Further sensitivity analyses for pure NG model improvement are shown in Figures 19 and 20. As noted earlier, experimental data points at each equivalence ratio are moderately faster than the NUIGMech 1.1 predictions. A change in the rate coefficient (*k*) for a reaction that would linearly shift the model predictions toward the experimental data may match better. The reaction,

$$
CH_3 + O_2 = CH_3O + O \tag{R118}
$$

is shared for all baseline NG mixtures at high and low temperatures in the sensitivity analyses and would also equally shift each prediction closer towards the data since the normalized sensitivity coefficients are similar in magnitude at both 1250 and 1400 K. Upon investigation of (R118), the listed uncertainty in k is more than ±30% from work done by Srinivasan *et al*. [45], giving a large range of adjustability. (R118) is also only commonly shared amongst the pure NG mixture, which would not significantly affect the agreement of the model with mixtures containing H_2 and NH_3 addition. A brief investigation into solely decreasing the A-factor of (R118) by 30% decreased the IDTs by as much as 8%, depending on the mixture and temperature. More experimental data at alternative pressures and temperatures from proceeding studies and thorough chemical analyses are required to compare the model performance before any modifications can be made to the chemical kinetic mechanism.

Alternatively, decreasing *k* of the inhibiting reaction,

$$
2CH_3 (+M) = C_2H_6 (+M)
$$
 (R227)

may also bring the model closer in agreement and has been calculated with a $\pm 20\%$ in the work of Blitz *et al*. [46]. However, this reaction is not advised to be modified because it is commonly shared in the NG/H² and NG/NH³ mixtures, which are already mostly in agreement with the model.

Figure 20: Pure NG sensitivity analysis at 1400 K.

CHAPTER 5: SUMMARY

In this work, hydrogen and ammonia addition to natural gas mixtures ignition was probed under gas turbine operating conditions. Equal amounts of hydrogen and ammonia were added to undiluted, pre-mixed mixtures of natural gas/air and combusted at the conditions relevant to current gas turbine operating conditions (1000-1500 K, 25 bar). The ignition delay times are reported here within and compared to the NUIGMech 1.1 for undiluted, high-fuel validation. Similar studies of undiluted NG mixtures have yet to be performed, but comparisons are made to fundamental work by De Vries and Petersen [17] as well as Baker *et al*. [20], who have performed relevant work. The work performed in this study is an initial step towards lowering carbon emissions for current NG turbines. The main conclusions of the study are as follows:

1. The NUIGMech 1.1 model shows good agreement for stoichiometric conditions but deviates during lean and rich conditions. Previously, undiluted chemistry effects on ignition at higher pressures were not explored but are now validated for chemical kinetic modeling. Pure NG measurements were moderately faster than the predictions, making a further analysis into relating reaction coefficients a necessary step to improve the model.

2. 50% H² fuel fraction greatly decreases IDT while NH³ shows to have no effect at the tested conditions. An analysis of the reactions in the ignition process shows dominating hydrogen chemistry for mixtures containing H_2 and dominating hydrocarbon chemistry for mixtures containing NH₃. While validation of emissions formation of CO and NO_x is still imperative, from an ignition standpoint, $NH₃$ addition looks like a promising and favorable modification to current NG turbines without needing a major infrastructure change.

3. Sensitivity analyses show large differences in the sensitive coefficient between stoichiometric pure NG and NG/H2. Stoichiometric NG/NH³ share very similar sensitivity coefficients with pure NG, further supporting that hydrocarbon chemistry dominates ignition rather than inhibiting nitrogen chemistry. The reaction $CH_3 + O_2 = CH_3O + O$ is suggested as a modifiable parameter to improve the model performance of pure NG, although not necessary for predicting H² and NH³ ignition.

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